

Through what angle in degrees does a 45 rpm record turn in 1.5 s?

7 inch format



$$\Theta = \omega \cdot t$$

$$\omega = 45 \text{ rpm} = (45 \cdot 2\pi)/60 \text{ sec} = 4.7 \text{ rad/s}$$

$$\Theta = (4.7 \text{ rad/s}) \cdot (1.5 \text{ s}) = 7.06 \text{ rad}$$

$$24,500 \text{ rev in 1 day}, \quad \omega = ?; \quad \omega = \frac{\Delta\theta}{\Delta t}$$

32. **ORGANIZE AND PLAN** The angular velocity is from Equation 8.3: $\omega = \Delta\theta/\Delta t$. We'll solve for this in both revolutions per minute and radians per second.

Known: $\Delta\theta = 24,500 \text{ rev}$, $\Delta t = 1 \text{ day}$.

SOLVE The angular displacement in radians is:

$$\Delta\theta = 24,500 \text{ rev} \left[\frac{2\pi \text{ rad}}{1 \text{ rev}} \right] = 1.54 \times 10^5 \text{ rad}$$

Solving Equation 8.3:

$$\begin{aligned} \omega &= \frac{24,500 \text{ rev}}{1 \text{ day}} \left[\frac{1 \text{ day}}{24 \cdot 60 \text{ min}} \right] = 17.0 \text{ rpm} \\ &= \frac{1.54 \times 10^5 \text{ rad}}{1 \text{ day}} \left[\frac{1 \text{ day}}{24 \cdot 60 \cdot 60 \text{ s}} \right] = 1.78 \text{ rad/s} \end{aligned}$$

REFLECT A rotation rate of 17 rpm may not sound all that fast, but hydroelectric turbines are typically a few meters in radius, so it would not be safe for them to turn as fast as a CD, for example.

5. If a wheel is turning at 3.0 rad/s, the time it takes to complete one revolution is about:

- 1) 0.33 s
- 2) 0.67 s
- 3) 1.0 s
- 4) 2.1 s

Answer

$$\frac{\theta}{t} = \frac{2\pi}{t} = 3 \frac{\text{rad}}{\text{s}} ; \theta = 2\pi = \omega \cdot t$$
$$T = t = \frac{2\pi}{\omega} = \frac{2 * 3.14 \text{ [rad]}}{3.0 \text{ [rad/s]}} = 2.1 \text{ s}$$

$$\omega = 43.8 \frac{\text{rad}}{\text{s}} \text{ after } 2.45 \text{ s } \quad \omega = 0 \quad \Delta t = ?$$

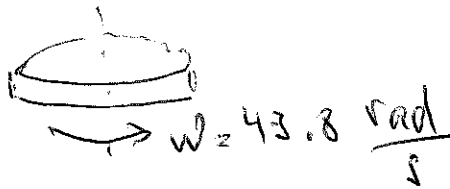
34. **ORGANIZE AND PLAN** The disk goes from 43.8 rad/s to 0 rad/s in 2.45 s. We can use Equation 8.6 to find the average angular acceleration: $\bar{\alpha} = \Delta\omega / \Delta t$.

Known: $\Delta\omega = 0 \text{ rad/s} - 43.8 \text{ rad/s} = -43.8 \text{ rad/s}$; $\Delta t = 2.45 \text{ s}$.

SOLVE Plugging the values into Equation 8.6:

$$\frac{\omega_f - \omega_i}{\Delta t} = \bar{\alpha} = \frac{\Delta\omega}{\Delta t} = \frac{(-43.8 \text{ rad/s})}{2.45 \text{ s}} = -17.9 \text{ rad/s}^2$$

REFLECT The acceleration is negative, as it should be, since the disk decelerates when the power is turned off due to friction.



27. A child, riding on a large merry-go-round, travels a distance of 3000 m in a circle of diameter 40 m. The total angle in radians through which she revolves is:

- 1) 50
- 2) 75
- 3) 150
- 4) 314

$$\text{Ans: } r = \frac{d}{2} = \frac{40}{2} = 20 \text{ m}$$

$$\frac{3000 \text{ m}}{2\pi r} = 23.8 \text{ rev}$$

$$23.8 \text{ rev} * (2\pi) = 150 \text{ rad}$$